

Closing Fri, Jan 8: 10.1

Closing Mon, Jan 11: 2.1

Closing Wed, Jan 13: 2.2

Closing Fri, Jan 15: 2.3

Go to course website and read
announcements and all postings.
(review sheets, unit circle, etc...)

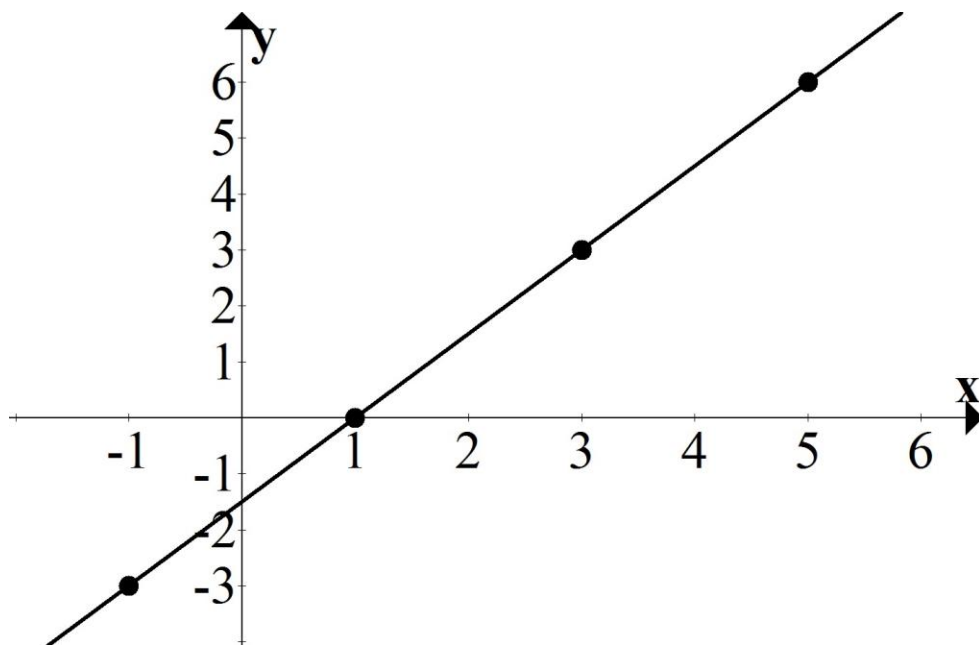
Today: **Parametric and Ch. 2 Intro**

Entry Task: (Uniform linear motion)

Consider $x = 1 + 2t$, $y = 3t$

- (1) Plug in $t = -1$ to get an (x,y) point.
Do the same for $t = 0, 1, \text{ and } 2$.
- (2) Plot these (x,y) points in the
 xy -plane and connect the dots.

t	$x = 1 + 2t$	$y = 3t$
-1	$x = 1 + 2(-1) = -1$	$y = 3(-1) = -3$
0	$x = 1 + 2(0) = 1$	$y = 3(0) = 0$
1	$x = 1 + 2(1) = 3$	$y = 3(1) = 3$
2	$x = 1 + 2(2) = 5$	$y = 3(2) = 6$

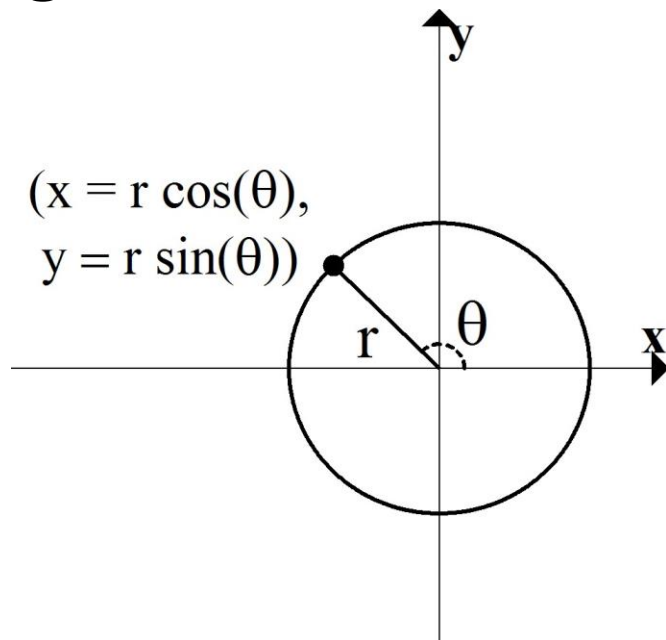


Since $x = 1 + 2t$, we have $t = \frac{1}{2}(x-1)$.

So $y = 3t = \frac{3}{2}(x-1)$ is the equation of the line's path.

Uniform Circular motion

Remember the fundamental connection between trig and circles:



If an object is traveling at a constant speed around a circle, then we first have to find θ before we can use the fact above.

Note: $\theta = \omega t + \theta_0$, where

θ_0 = the starting angle (radians)

ω = angular speed (rad/time)

t = time

Example:

A bug runs along a circular path that is 7 inches in radius. It starts at the west-most edge and rotates counterclockwise at a constant 10 revolutions per minute. Give the equations for motion in terms of time t .

$$r = ??$$

$$\theta_0 = ?? \quad (\text{give in radians})$$

$$\omega = ?? \quad (\text{give in radians/min})$$

Ch. 2 Limits and Derivatives

2.1 Motivation

The foundation of calculus is “limiting processes”, where a procedure “approaches the exact answer” through better and better approximations.

Calculus is also primarily about “rates”.
It could be called the study of rates.

Recall:

$$\text{rate} = (\text{change in quantity})/(\text{change in time})$$

Example: The distance traveled by an object is recorded at various times:

t (seconds)	0	1	2	3
Dist (meters)	0	1.2	4.5	10.4

1. What is the average velocity from $t = 1$ to $t = 3$?
2. What is the average velocity from $t = 2$ to $t = 3$?
3. What is the instantaneous velocity at $t = 3$?